

# Price Responsive Demand for Operating Reserves in Co-Optimized Electricity Markets with Wind Power

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# Outline

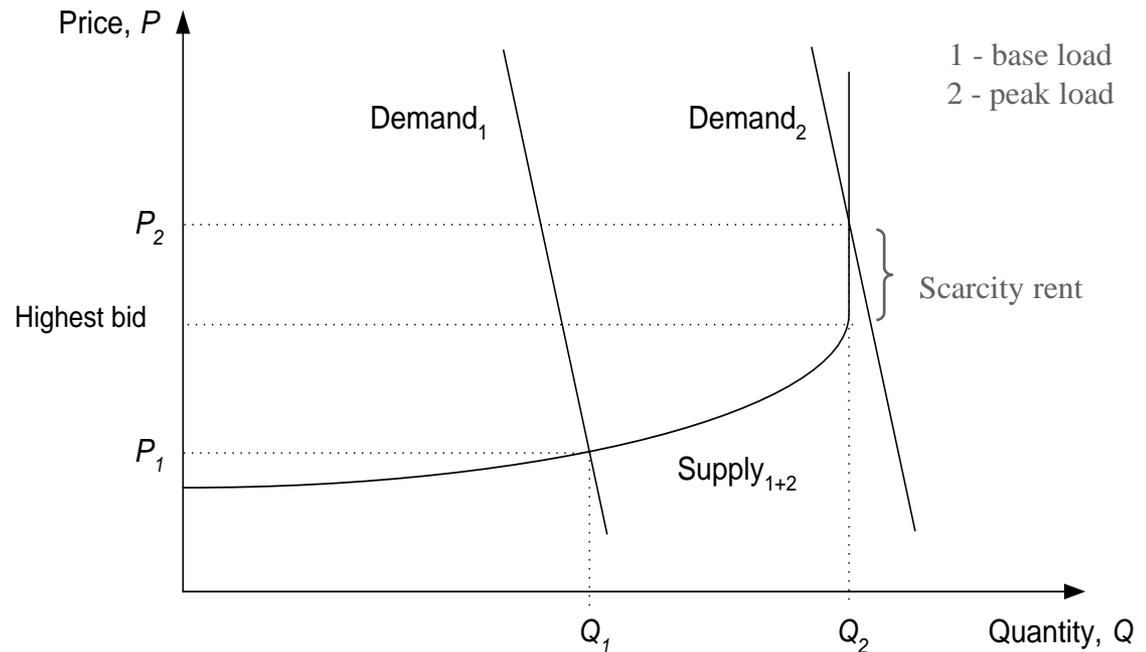
- Background and Motivation
  - Scarcity pricing in electricity markets
  - Wind power uncertainty in market operations
- Analytical approach
  - Wind power forecast uncertainty
  - Demand curve for operating reserves
  - Market operations: commitment and dispatch
- Case study of IL power system
  - Assumptions
  - Costs, prices, revenue
- Concluding Remarks



# Prices and Investments in the Electricity Market

In a perfect market:

- Scarcity rent covers investment costs for the optimal mix of new generation
- Investments should come in time to meet demand



Source: Botterud 2003

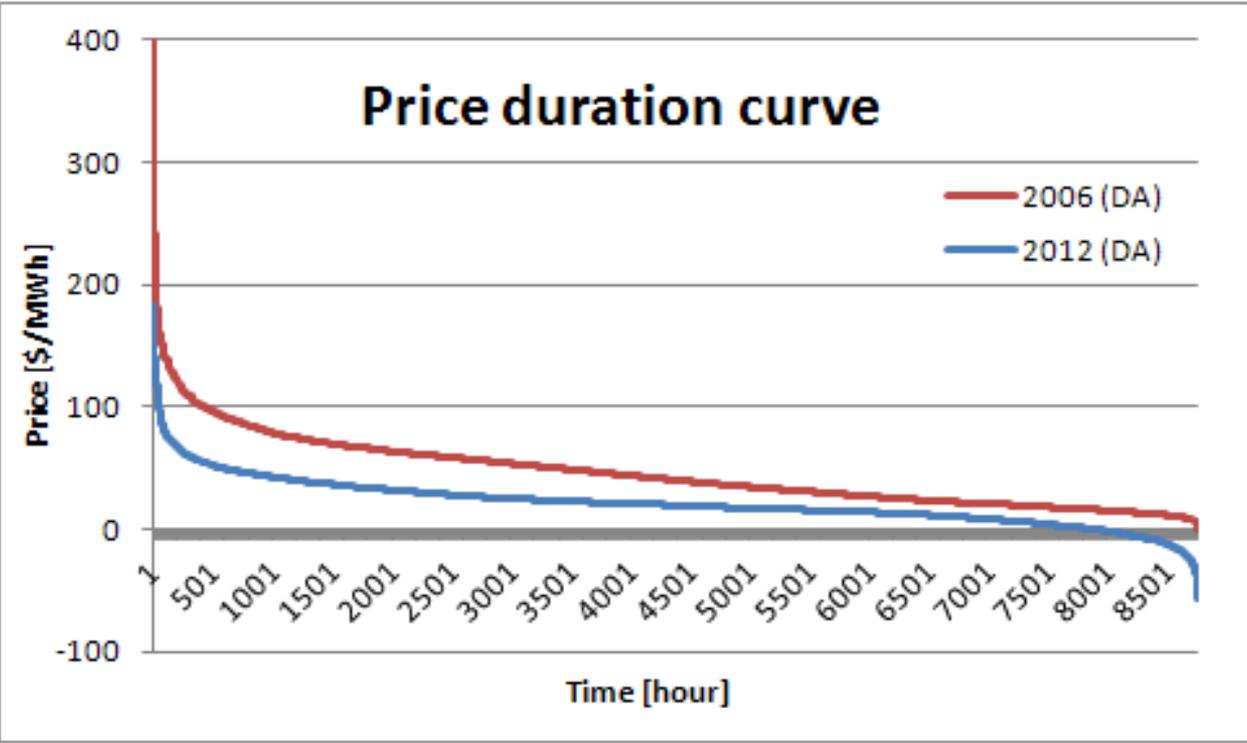
Potential problems for adequate generation investments:

- Limited demand response, price caps and poor scarcity pricing (“missing money”), high investment risks difficult to hedge, market power
- *How does a large-scale wind power expansion influence investments?*
  - *Resource variability and ramping, forecast uncertainty, low marginal costs*



# Electricity Prices in MISO node 2006 and 2012

- Historical day-ahead prices for ALTW.FOXLK1 node in Lakefield, MN

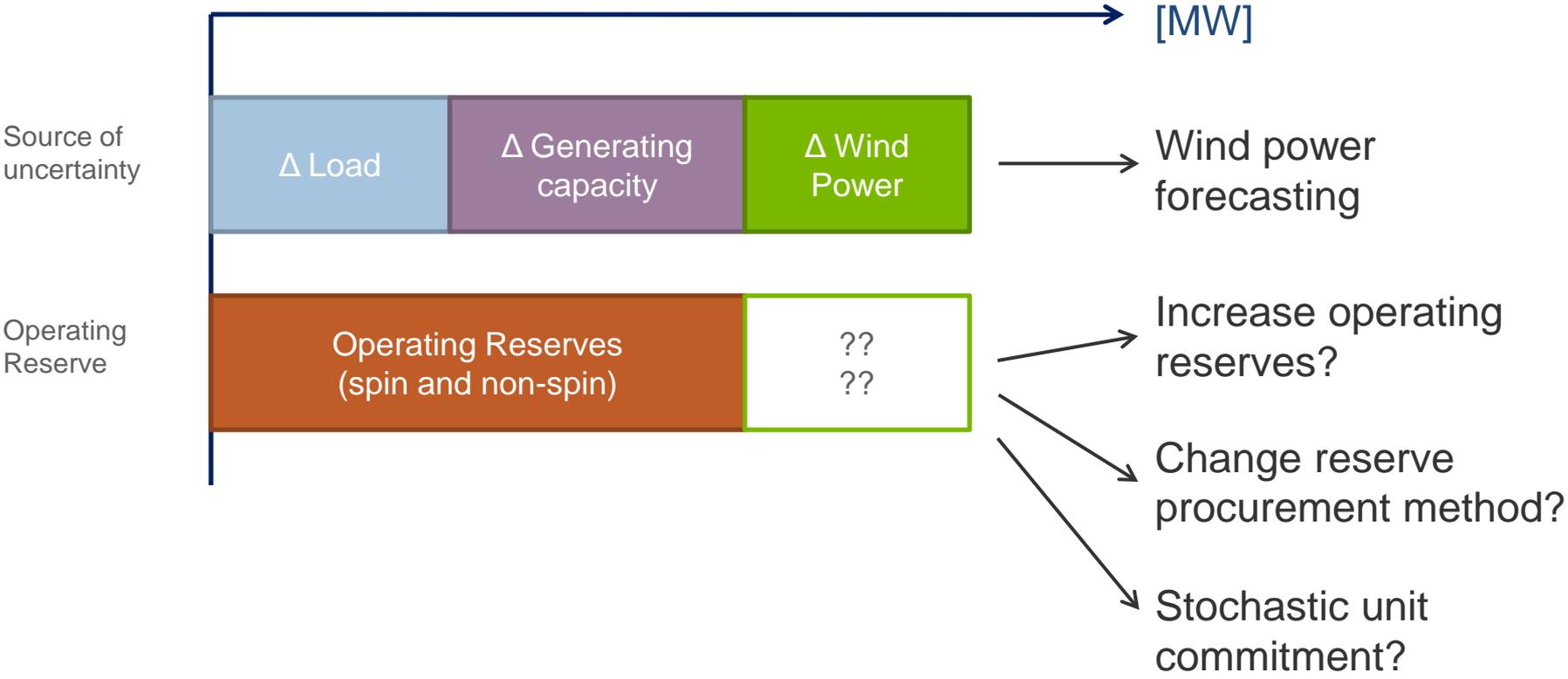


Price	2006	2012
Average [\$/MWh]	46.1	21.3
Rel. St.Dev. [%]	64.0	92.3

*Wind power increases the need for adequate scarcity pricing*



# Handling Uncertainties in System/Market Operation



*A demand curve for operating reserves can address forecast uncertainty in short-term operations and improved scarcity pricing for long-term resource adequacy*



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# Probabilistic Forecasting - Kernel Density Estimation

## Conditional wind power probabilistic forecasting

$$f_P(p_{t+k} | X = x_{t+k|t}) = \frac{f_{P,X}(p_{t+k}, x_{t+k|t})}{f_X(x_{t+k|t})}$$

Joint or multivariate density function of  $p$  and  $x$

Marginal density of  $x$

## Kernel density estimation (KDE)

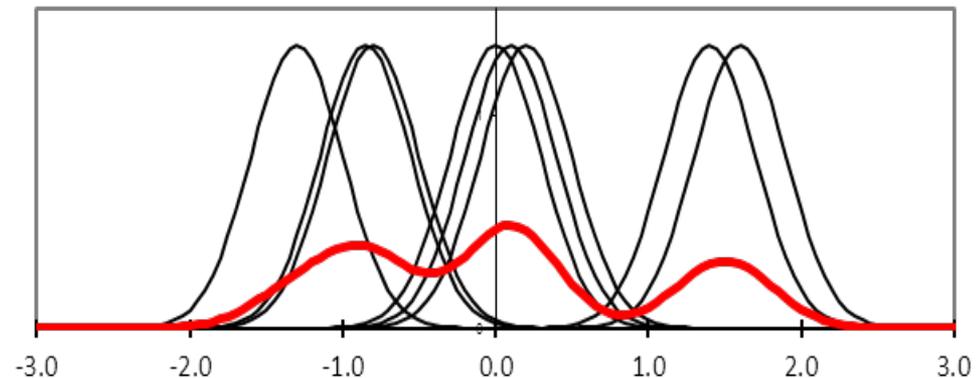
### – Advantages

- Forecasts the full probability density function
- Nonparametric

### – Example

$$\hat{f}_X(x) = \frac{1}{N} \cdot \sum_{i=1}^N \frac{1}{h_i} \cdot K\left(\frac{x - X_i}{h}\right)$$

$$K(x) = \frac{1}{N} \cdot \sum_{i=1}^N \frac{1}{\sqrt{2\pi}} \cdot e^{-\frac{(x-X_i)^2}{2 \cdot h^2}}$$



# Probabilistic Forecasting - Quantile-Copula Estimator

Copula Definition

$$F_{XY}(x, y) = C(F_X(x), F_Y(y))$$

multivariate distribution function separated in:

- marginal functions
- dependency structure between the marginals modeled by a copula

$$f(x, y) = \frac{\partial^2}{\partial u \cdot \partial v} \cdot C(u, v) = f_X(x) \cdot f_Y(y) \cdot c(u, v)$$

copula density function

$$f(y|X = x) = \frac{f_X(x) \cdot f_Y(y) \cdot c(u, v)}{f_X(x)} = f_Y(y) \cdot c(u, v)$$

KDE ESTIMATOR

$$\hat{f}_Y(y) = \frac{1}{N} \cdot \sum_{i=1}^N \frac{1}{h_i} \cdot K\left(\frac{y - Y_i}{h_y}\right)$$

KDE ESTIMATOR

$$\hat{c}(u, v) = \frac{1}{N} \sum_{i=1}^N K\left(\frac{u - U_i}{h_u}\right) \cdot K\left(\frac{v - V_i}{h_v}\right)$$

empirical cum. dist.

$$F^E(t) = \frac{1}{N} \cdot \sum_{i=1}^N I(x_i \leq t)$$

$U_i = F_X^e(X_i)$  and  $V_i = F_Y^e(Y_i)$

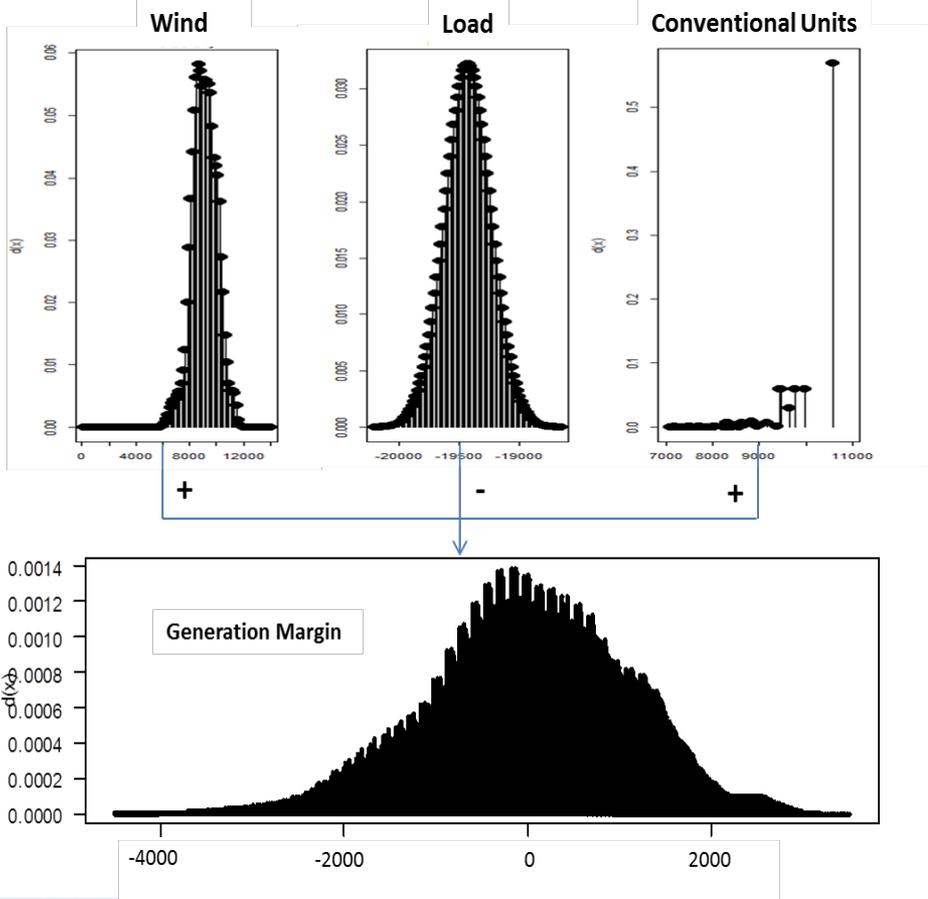
$$\hat{f}(y|X = x) = \frac{1}{N \cdot h_y} \cdot \sum_{i=1}^N K_y\left(\frac{y - Y_i}{h_y}\right) \cdot \frac{1}{N} \cdot \sum_{i=1}^N K_u\left(\frac{F_X^e(u) - F_X^e(U_i)}{h_u}\right) \cdot K_v\left(\frac{F_X^e(v) - F_X^e(V_i)}{h_v}\right)$$

[Bessa et al. 2012]

# Demand Curve for Operating Reserves – Overview

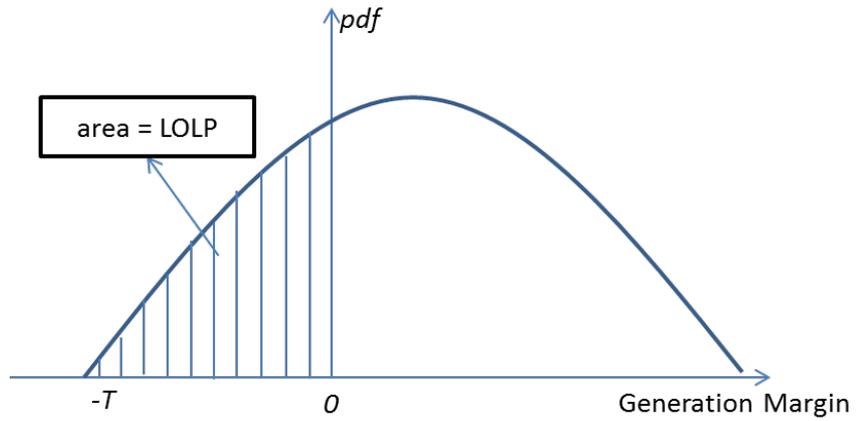
- Basic idea
  - Consider the uncertainties from load and supply (thermal and wind)
  - Estimate the risk of supply shortage for system
  - Link the expected cost of this risk to the price to pay for reserves (Hogan, 2005)

- Uncertainty sources:
  - Wind power: probabilistic forecast
  - Load: forecasting error
  - Thermal units: forced outage rates



# From Generation Margin to Demand Curve

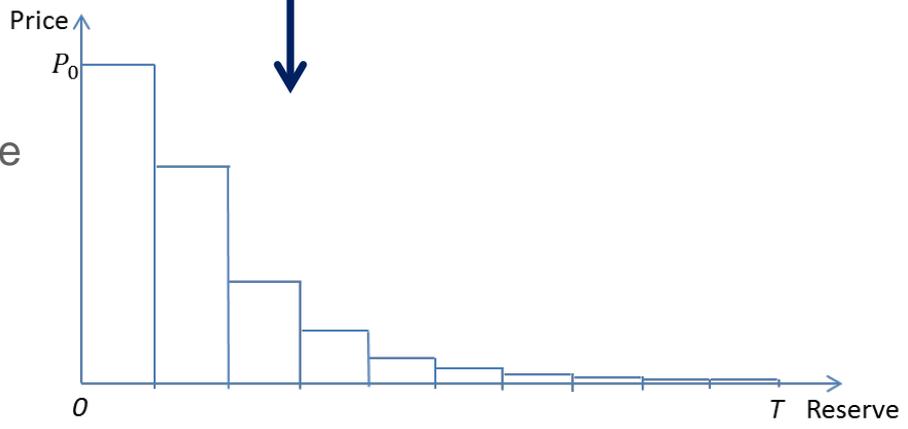
Generation Margin Distribution



LOLP: Loss of load probability  
VOLL: Value of loss load

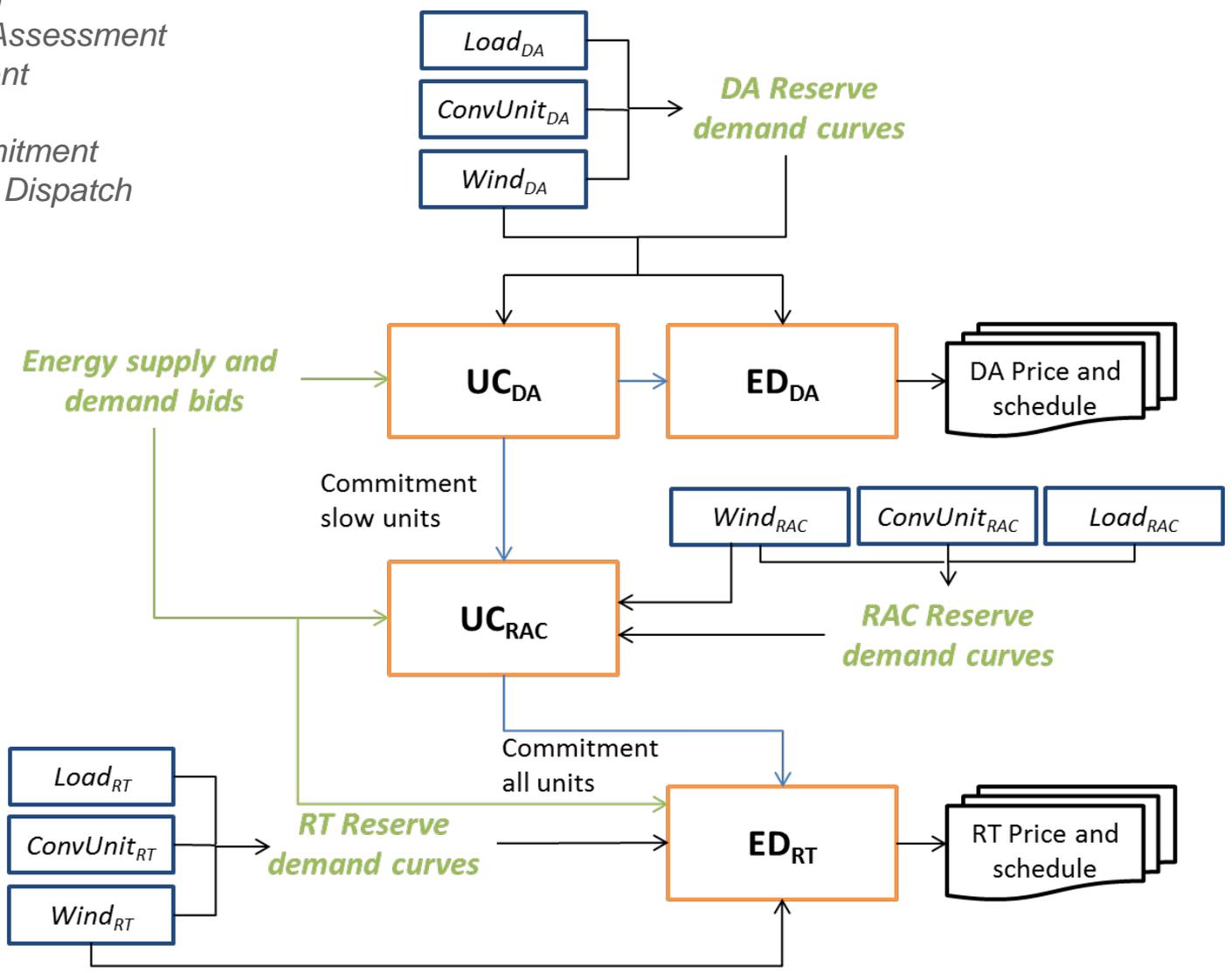
$$Price(reserve) = LOLP(reserve, gen.margin) * VOLL$$

Stepwise Operating Reserve Demand Curve



# Simulating Electricity Market Operations

DA: Day-ahead  
 RAC: Reliability Assessment  
 Commitment  
 RT: Real Time  
 UC: Unit Commitment  
 ED: Economic Dispatch



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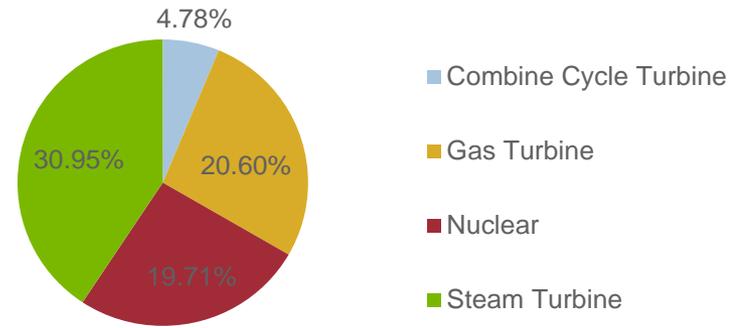
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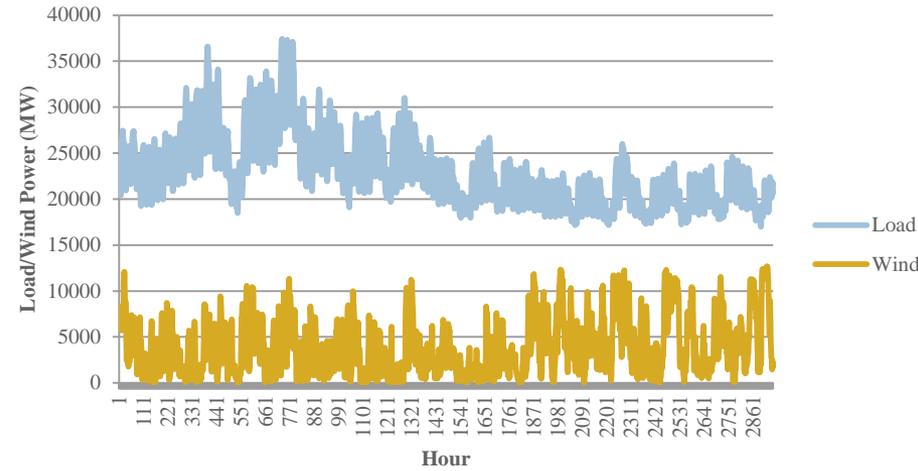
# Case Study Assumptions

- **210 thermal units: 41,380 MW**
  - Base, intermediate, peak units
- **Peak load: 37,419 MW**
  - 2006 load series from Illinois
- **Wind power: 14,000 MW**
  - 2006 wind series from 15 sites in Illinois (NREL EWITS dataset)
  - 20% of load
- **Simulation periods**
  - (1) High load period (July); (2) Low load period (Oct)
- **Curtailement assumptions**
  - Value of Lost Load: \$3500/MWh
  - Value of operating reserve shortfall: \$1100/MWh

## Generation Capacity



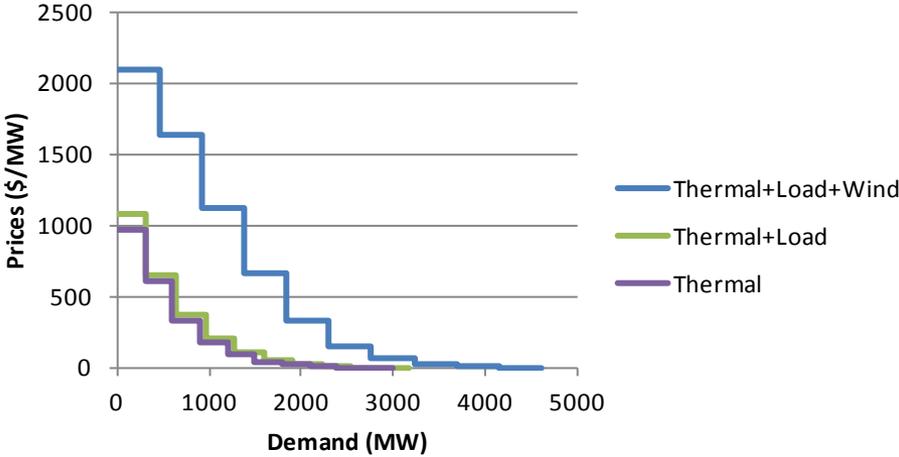
Wind and Load in July-October 2006



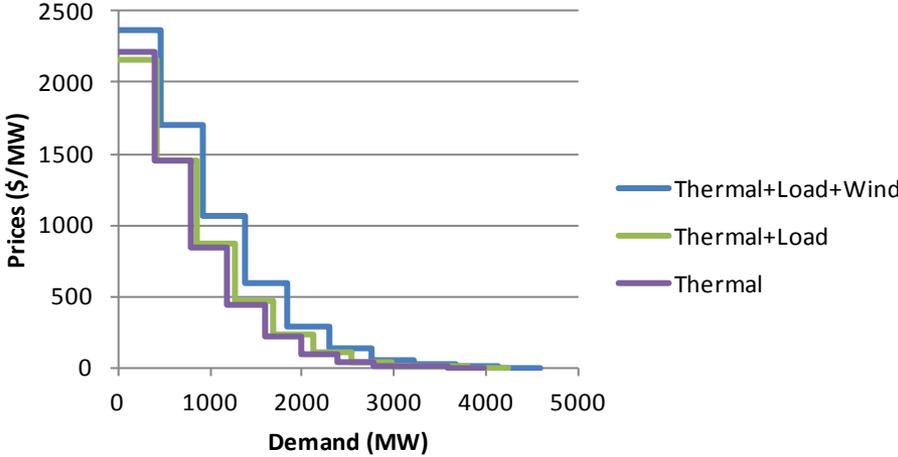
# Demand for Operating Reserves is Dynamic

- Demand curve examples
  - Hourly demand curves for the sum of spinning and non-spinning reserves
  - Contributions to reserve demand for two selected hours:

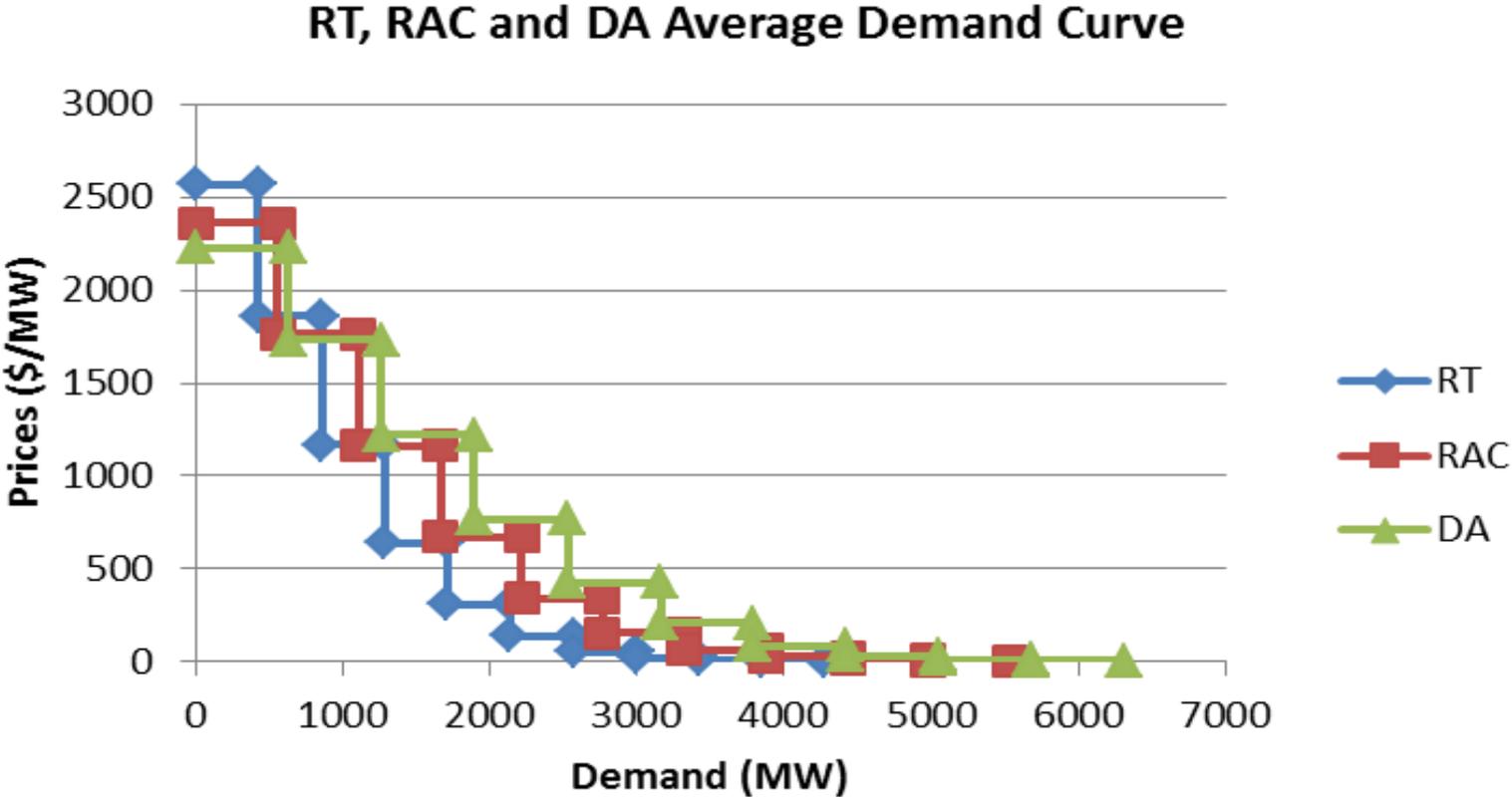
Low Load and High Wind Power Uncertainty



High Load and Low Wind Power Uncertainty



# Average OR Demand in July



- Total demand for reserves is higher in DA than in RAC and RT.

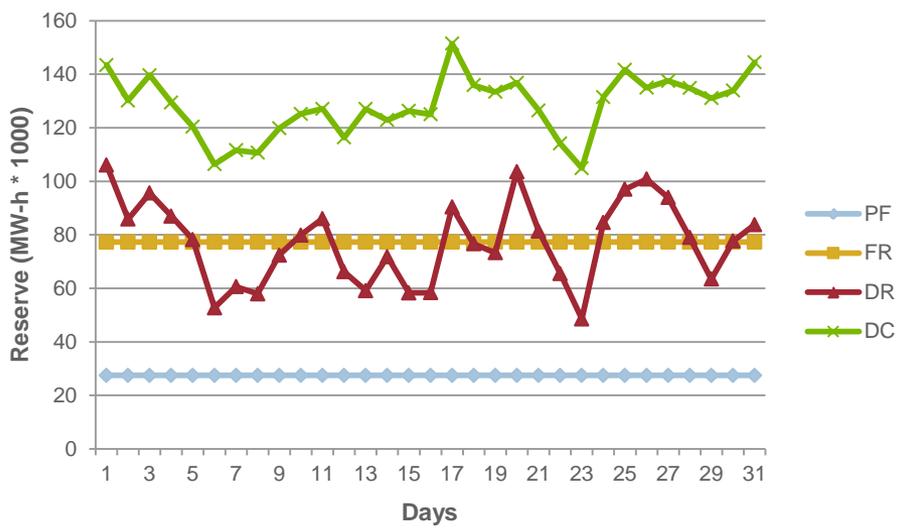
# Simulated Cases

Case	Description	Wind power forecast	Operating reserves		
			Generator contingency	Load forecast error	Wind forecast error
PF	Perfect forecast	Perfect	1146 MW	No	No
FR	Fixed reserve	50 % quantile	1146 MW	No	Avg. 50-1 quant.
DR	Dynamic reserve	50 % quantile	1146 MW	No	50-1 quant.
DC	Demand curve	50 % quantile	Joint demand curve		

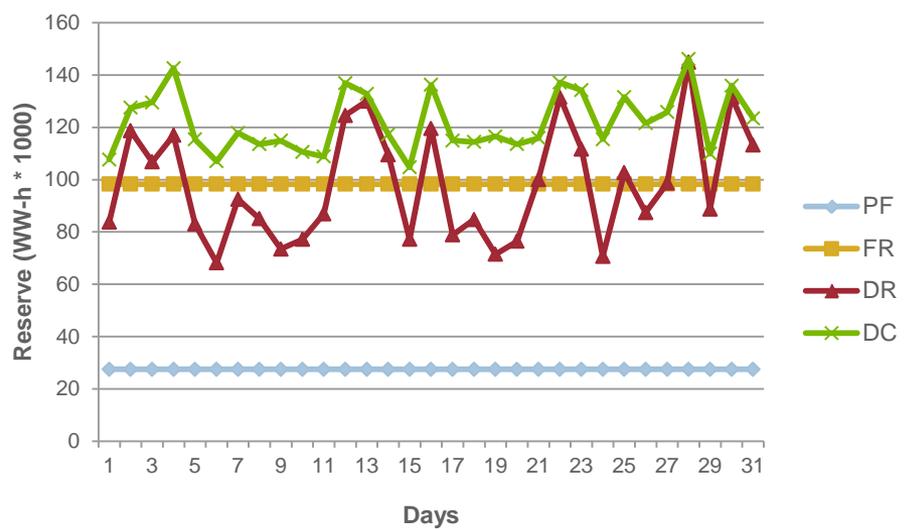


# Impact on Operating Reserves Schedule

July DA Reserve Scheduled



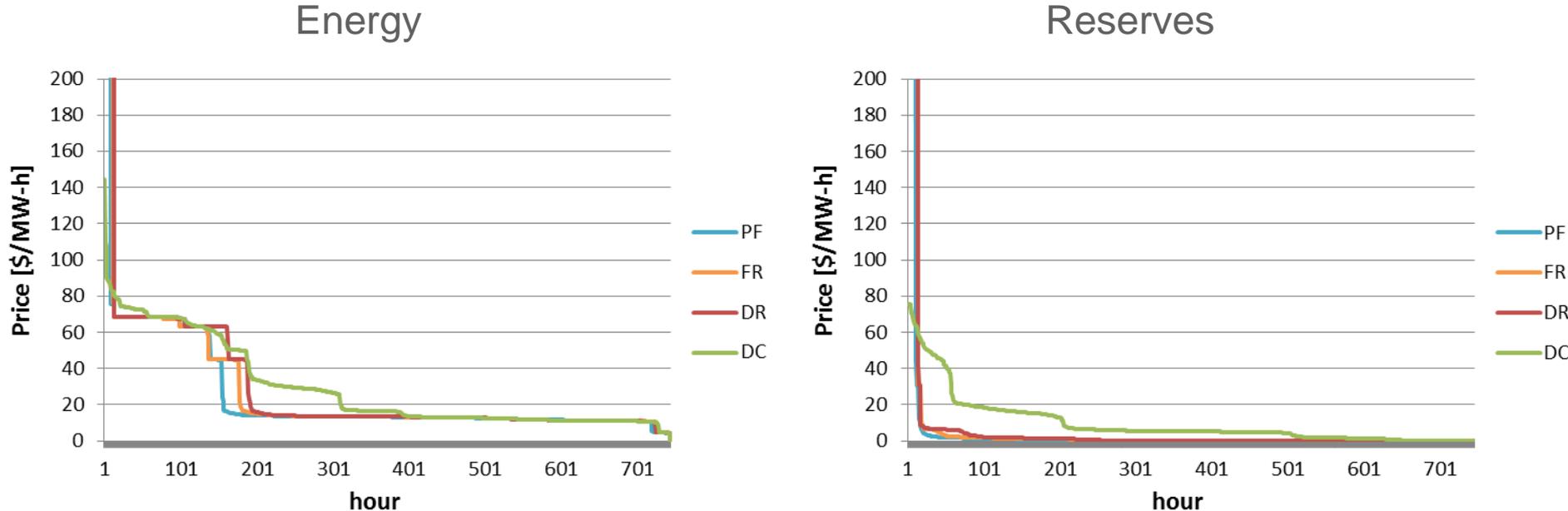
Oct DA Reserve Scheduled



- The demand curve tends to schedule more operating reserves

# Implications for Energy and Reserves Prices

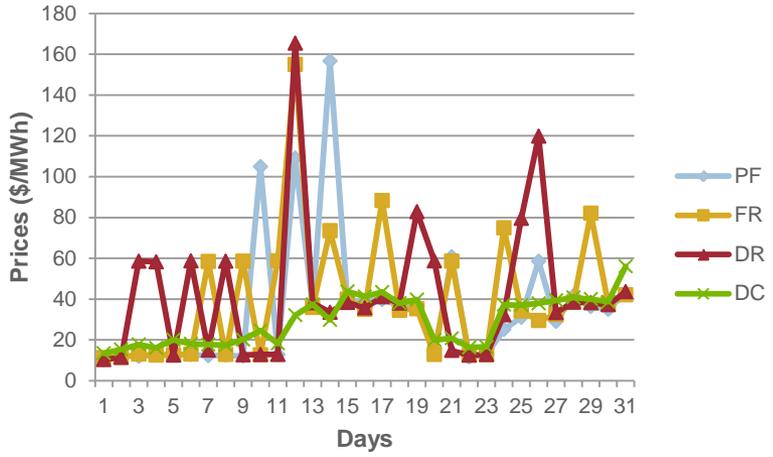
Price duration curves for day-ahead market, month of July:



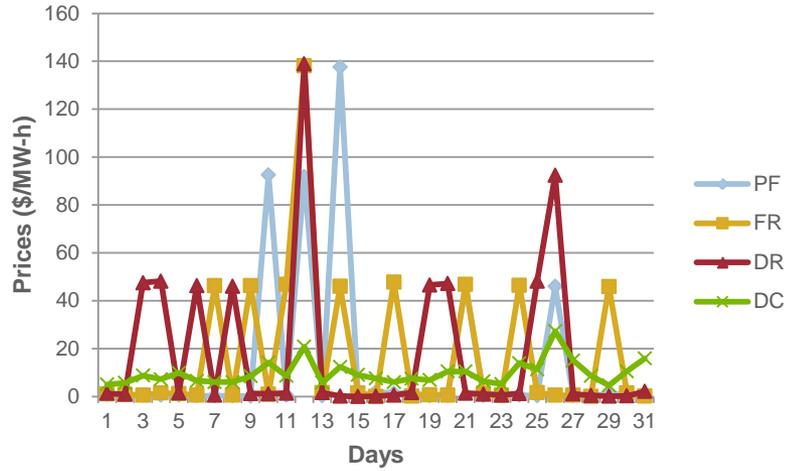
- A demand curve for operating reserves
  - Gives higher prices for energy and reserves in most hours, fewer extreme price spikes
  - Stabilizes revenue stream for thermal generators; can alleviate “missing money” problem
  - Better reflects wind power forecast uncertainty in prices

# Average Daily Operating Reserves Prices

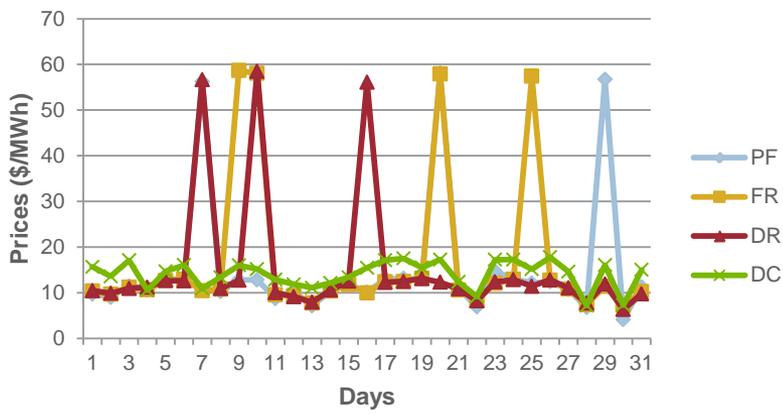
July DA Average Daily Energy Prices



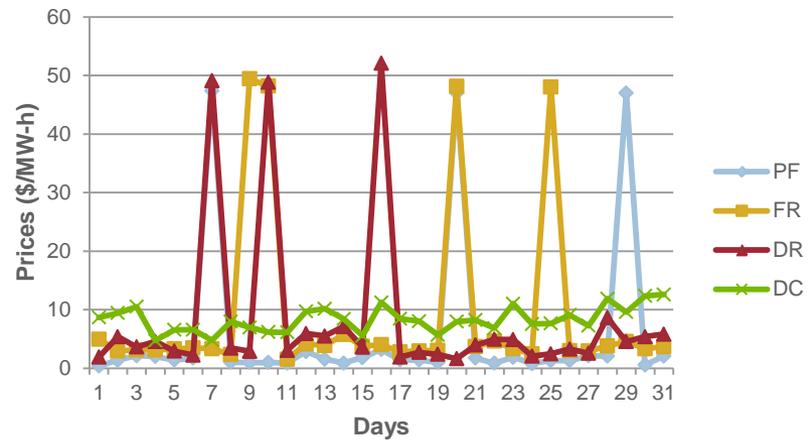
July DA Average Daily Reserve Prices



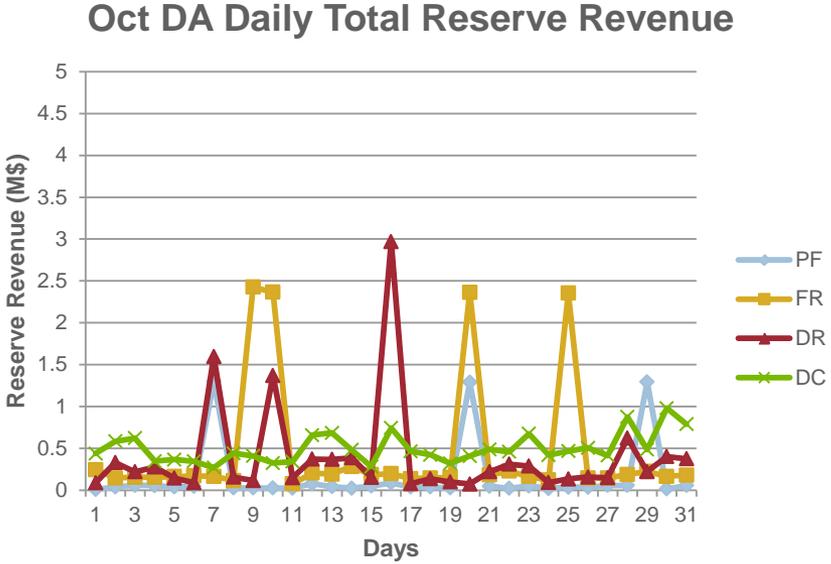
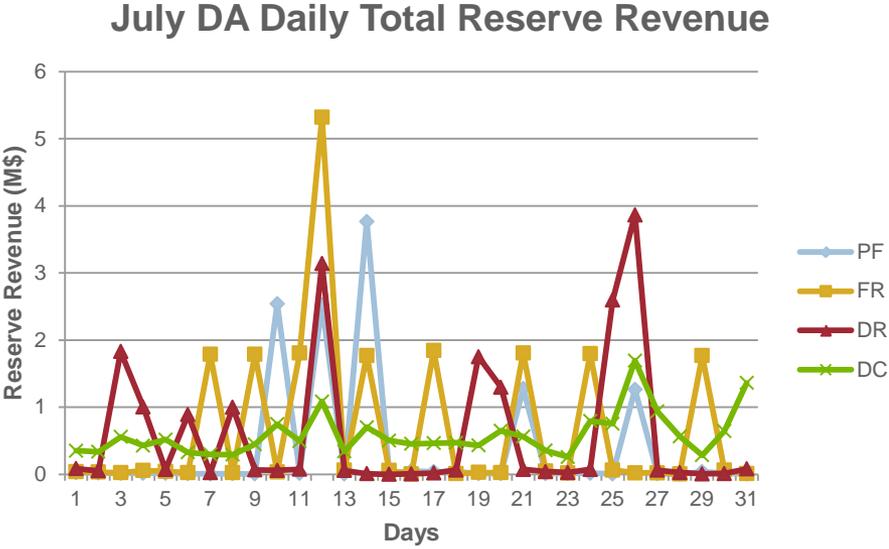
Oct DA Average Daily Energy Prices



Oct DA Daily Average Reserve Prices



# Impact on Operating Reserve Revenue



■ A demand curve for operating reserves stabilizes the revenue stream

# Overview of Total Operating Cost

- High load period (July)

RT-Cost (M\$)	PF	FR	DR	DC
<b>Total</b>	198.74	212.91	209.02	215.07
<b>Fuel</b>	189.39	202.08	199.58	207.03
<b>Startup</b>	9.33	9.67	8.93	8.04
<b>Curtailement</b>	0.02	1.16	0.51	NA

- Low load period (October)

RT-Cost (M\$)	PF	FR	DR	DC
<b>Total</b>	96.46	117.68	115.71	110.67
<b>Fuel</b>	89.63	106.31	107.93	102.30
<b>Startup</b>	6.83	8.57	7.58	8.37
<b>Curtailement</b>	0.00	2.80	0.20	NA



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# Conclusion and Future Work

## ■ A demand curve for operating reserves

- Provides prices that better *reflect the marginal reliability* of the system as a function of the reserve level, accounting for multiple uncertainties (load, outages, wind).
- Contributes towards *more efficient market operations* through improved price signals for short-term operation and maintenance, and long-term system expansion.
- Is a solution that *is compatible with current market designs*.
- Tends to schedule more reserves than price-inelastic reserve requirements in case study.

## ■ Future work

- Introduce transmission network / locational operating reserve demand curves.
- Reserve provision from wind power and demand.
- Supply curves from ancillary service providers.



# References and Acknowledgements

## ■ References for more information

- Zhou Z., Botterud A., “Price Responsive Demand for Operating Reserves and Energy in Electricity Markets with Wind Power,” IEEE Power & Energy Society Annual Meeting, Vancouver, Canada, July 2013.
- Zhou Z., Botterud A., Wang J., Bessa R.J., Keko H., Sumaili J., Miranda V., “Application of Probabilistic Wind Power Forecasting in Electricity Markets,” *Wind Energy*, Vol. 16, No. 3, pp.321-338, 2013.
- Bessa R.J., Miranda V., Botterud A., Zhou Z., Wang J., “Time-Adaptive Quantile-Copula for Wind Power Probabilistic Forecasting,” *Renewable Energy*, Vol. 40, No. 1, pp. 29-39, 2012.

## ■ Acknowledgements

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Project website: <http://www.dis.anl.gov/projects/windpowerforecasting.html>



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